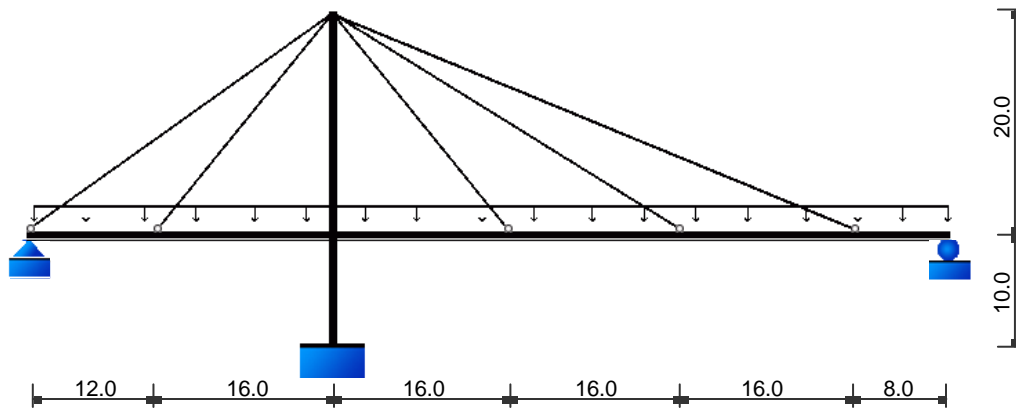


## Advanced Application 8

Example of Unknown Load Factors using  
Forward Construction Stage Analysis  
(for illustrative purposes only)

## 8.1 Example Model Dimensions

For an asymmetrical cable-stayed bridge as shown in Figure 1, we will find pretension loads for each construction stage by using the Unknown Load Factors feature, reflecting Forward Construction Stage Analysis.



**Figure 1. Configuration at the final stage of an asymmetrical cable-stayed bridge**

**Table 1. Material data of the example model**

| Classification | Modulus of Elasticity | Poisson's Ratio |
|----------------|-----------------------|-----------------|
| Deck           | 3.0000e+006           | 0.3             |
| Pylon          | 3.0000e+006           | 0.3             |
| Cable          | 1.5750e+007           | 0.3             |

**Table 2. Section data of the example model**

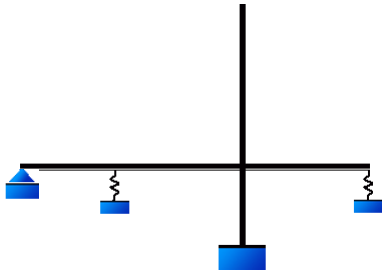
| Classification | Cross-sectional Area | Moment of Inertia |
|----------------|----------------------|-------------------|
| Deck           | 4.3800               | 0.9200            |
| Pylon          | 1.0000               | 2.7600            |
| Cable          | 0.0062               | -                 |
| Cable          | 0.0208               | -                 |

**Table 3. Loading data of the example model**

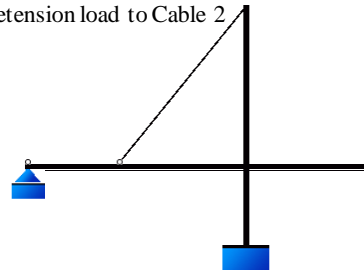
| Classification                            | Load Type              | Load Value  |
|---|------------------------|---|
| Dead load                                 | Self weight            |   |
| Cable pretension load                     | Pretension Loads       | 1 tonf  |
| Derick Crane                              | Nodal Loads            | 80 tonf   |
| Segment                                   | Nodal Loads            | Gravity load: $A \times \gamma \times L$<br>Eccentric Moment: $A \times \gamma \times L \times L/2$ |
| Superimposed (2 <sup>nd</sup> ) dead load | Element Beam Loads     | 1 tonf/m  |
| Support movement                          | Specified displacement | 1 mm  |

## 8.2 Construction Sequence

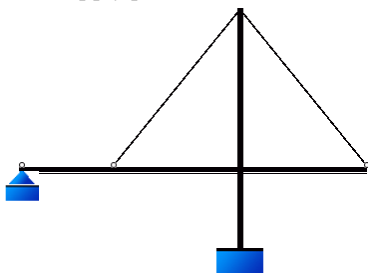
CS1: Erect Pylon and Deck



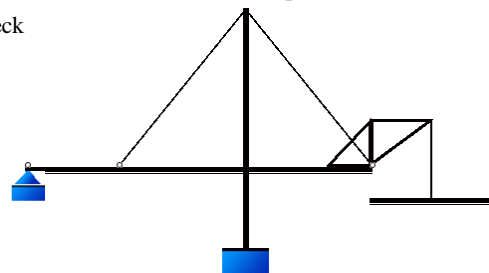
CS2: Remove temporary supports and apply pretension load to Cable 2



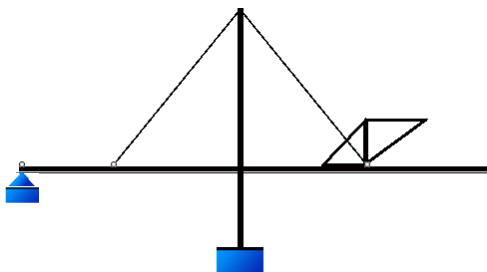
CS3: Apply pretension load to Cable 3



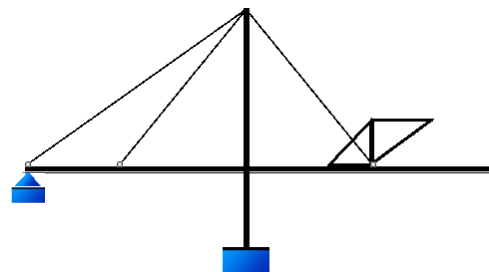
CS4: Install Derrick Crane and place loads to Deck



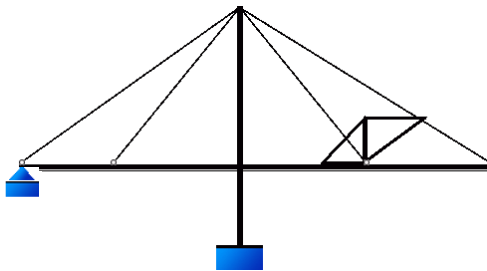
CS5: Construct additional Deck



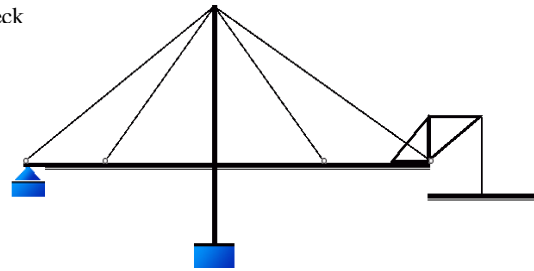
CS6: Apply pretension load to Cable 1



CS7: Apply pretension load to Cable 4

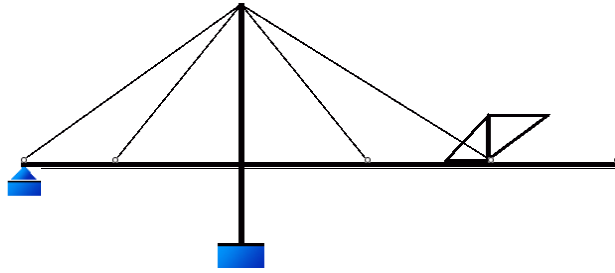


CS8: Move Derrick Crane and place loads to Deck

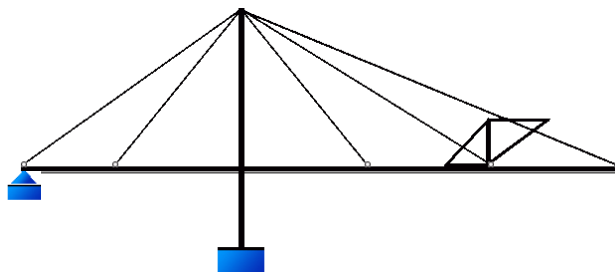


**Figure 2. Construction Stages for the example model (CS1 ~ CS14)**

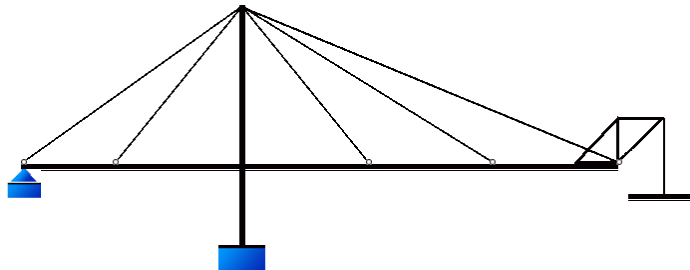
CS9: Construct additional Deck



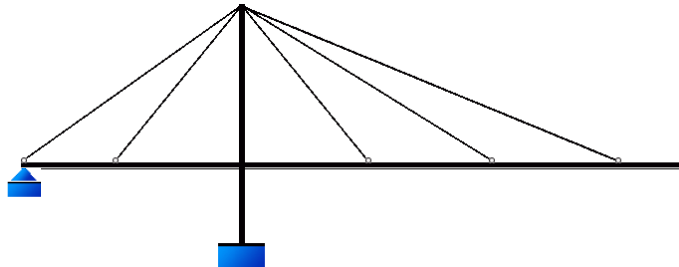
CS10: Apply pretension load to Cable 5



CS11: Move Derick Crane and place loads to Deck

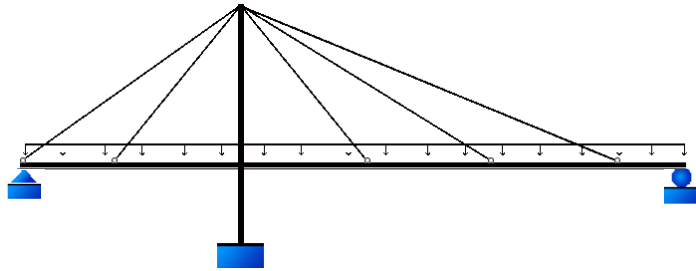


CS12: Construct additional Deck

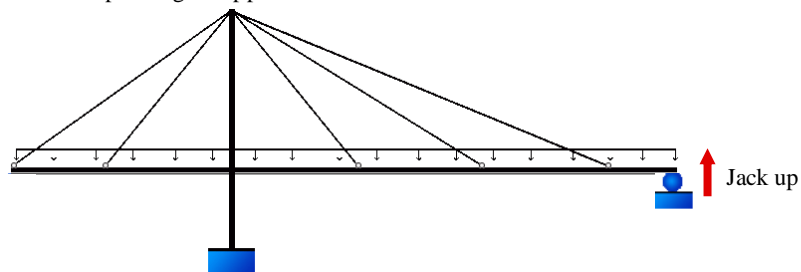


**Figure 2 Construction Stages for the example model (CS1 ~ CS14) (Continued..)**

CS13: Construct a support at the right span and place 2<sup>nd</sup> dead loads



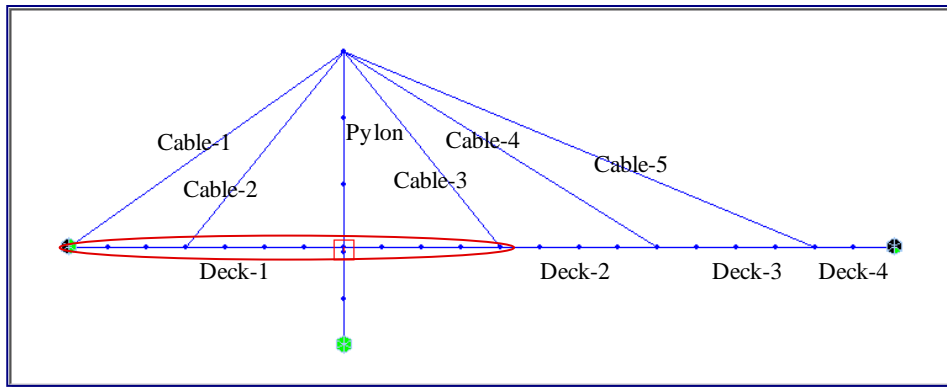
CS14: Jack up the right support



**Figure 2 Construction Stages for the example model (CS1 ~ CS14) (Continued..)**

### 8.3 Generating a Construction Stage Analysis Model

Construction consists of 14 stages, and the stages are defined in Table 4.



**Figure 3. Structure Group names used for the example model**

**Table 4. Defining construction stages for the example model**

| Stage        | Structure       |              | Boundary                                       |              | Load: Step                     |                                |
|--------------|-----------------|--------------|--|--------------|--------------------------------|--------------------------------|
|              | Activation      | Deactivation | Activation                                     | Deactivation | Activation                     | Deactivation                   |
| <b>CS 1</b>  | Deck-1<br>Pylon | -            | Deck-Left<br>Pylon<br>Elastic Sup<br>Temporary | -            | Self weight: First             | -                              |
| <b>CS 2</b>  | Cable-2         | -            | -  | Temporary    | Tension 02: Last               | -                              |
| <b>CS 3</b>  | Cable-3         | -            | -  | -            | Tension 03: First              | -                              |
| <b>CS 4</b>  | -               | -            | -  | -            | D/C-04: First<br>Seg-04: First | -                              |
| <b>CS 5</b>  | Deck-2          | -            | -  | -            | -                              | Seg-04: First                  |
| <b>CS 6</b>  | Cable-1         | -            | -  | -            | Tension 06: First              | -                              |
| <b>CS 7</b>  | Cable-4         | -            | -  | -            | Tension 07: First              | -                              |
| <b>CS 8</b>  | -               | -            | -  | -            | D/C-08: First<br>Seg-08: First | D/C-04: First                  |
| <b>CS 9</b>  | Deck-3          | -            | -  | -            | -                              | Seg-08: First                  |
| <b>CS 10</b> | Cable-5         | -            | -  | -            | Tension 10: First              | -                              |
| <b>CS 11</b> | -               | -            | -  | -            | D/C-11: First<br>Seg-08: First | D/C-08: First                  |
| <b>CS 12</b> | Deck-4          | -            | -  | -            | -                              | D/C-11: First<br>Seg-08: First |
| <b>CS 13</b> | -               | -            | Deck-Right                                     | -            | -                              | -                              |
| <b>CS 14</b> | -               | -            | -  | -            | Jack Up                        | -                              |

(1) Construction Stage Analysis Model using MIDAS/Civil

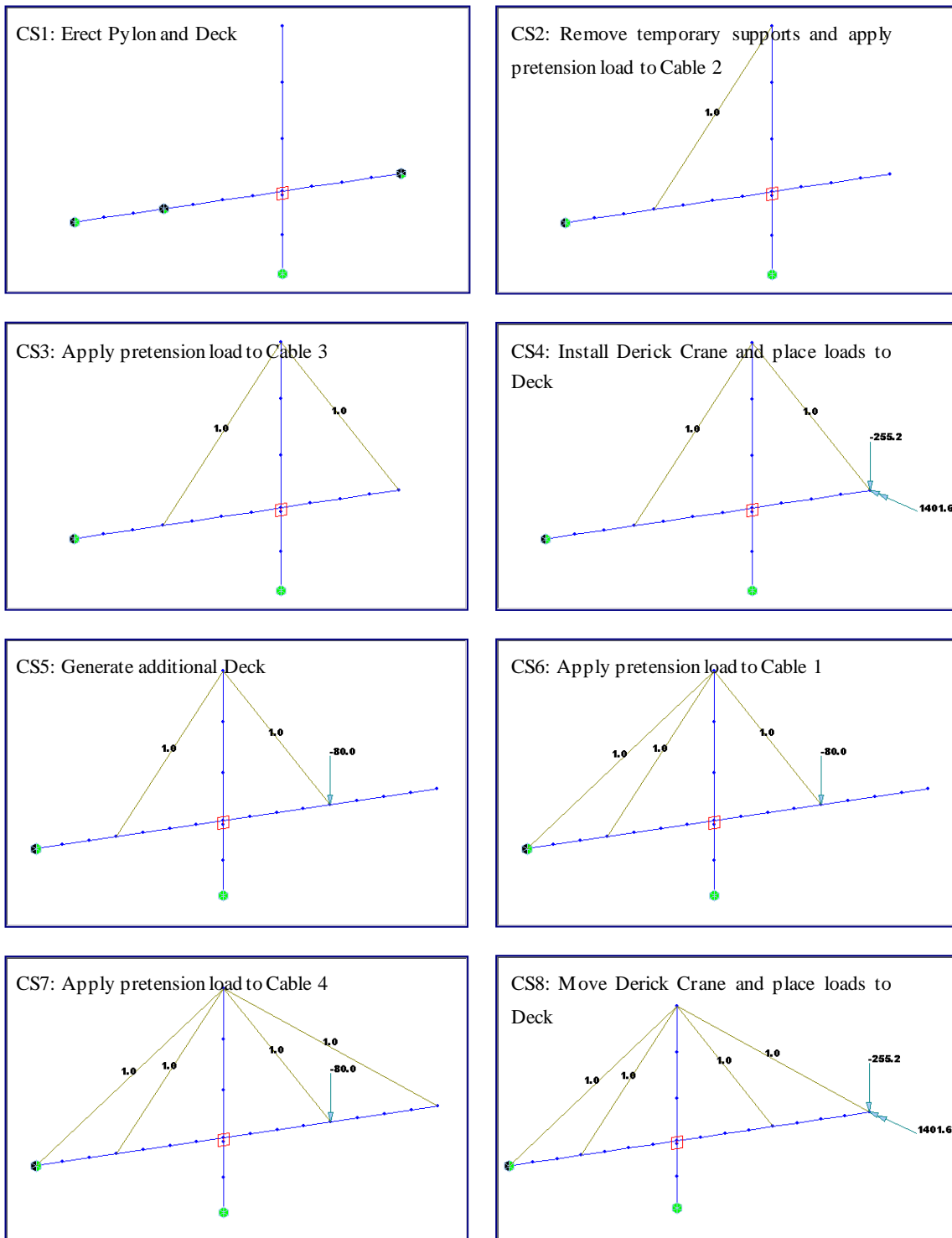


Figure 4. Construction Stage Analysis Model using MIDAS/Civil (CS1~CS14)

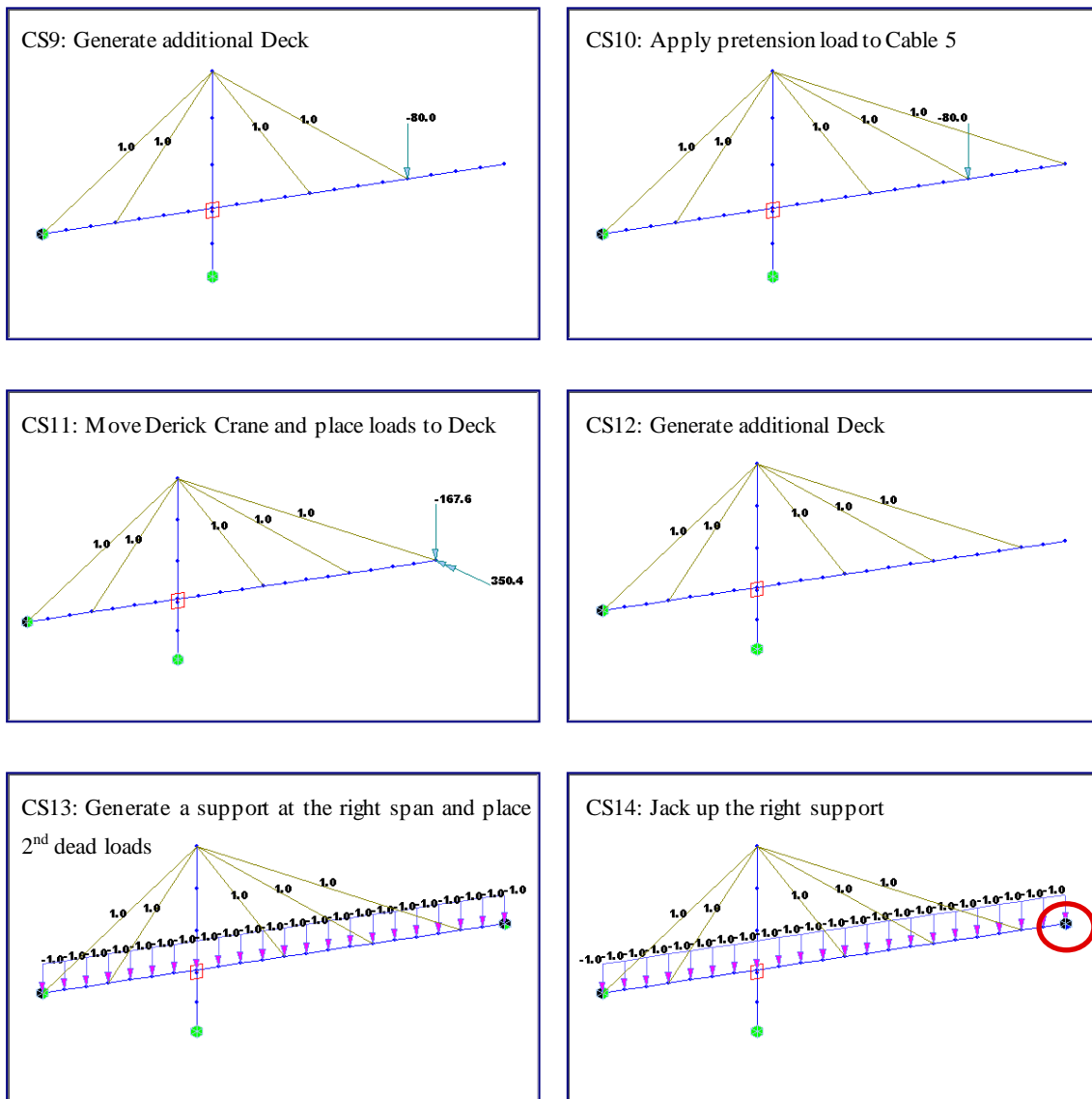


Figure 4. Construction Stage Analysis Model using MIDAS/Civil (CS1~CS14) (Continued..)

## 8.4 Input Data for Unknown Load Factors

- After construction stage analysis is complete, switch to Post CS.
- Select CS14, which is the final stage, for Stage Name.
- Select Stage/Steps at which cable pretension loads have been activated and a support has been jacked up (Figure 5).

Item Name:

Stage Name:

Object function type  
☐ Linear ☒ Square ☐ Max Abs

Sign of unknowns  
☐ Negative ☒ Both ☐ Positive

Constraints  
☒ Ele-03  
☒ Ele-07  
☒ Ele-11  
☒ Ele-15  
☒ Ele-19  
☒ Node106

|    | Unknown                             | Stage/Step      | Factor  | Weighted Factor | DL                                  | ER                                  |
|----|-------------------------------------|-----------------|---------|-----------------|-------------------------------------|-------------------------------------|
| 1  | <input type="checkbox"/>            | CS01.Last Step  | 1.000   |                 | <input type="checkbox"/>            | <input type="checkbox"/>            |
| 2  | <input type="checkbox"/>            | CS02.First Step | 1.000   |                 | <input type="checkbox"/>            | <input type="checkbox"/>            |
| 3  | <input checked="" type="checkbox"/> | CS02.Last Step  | Unknown | 1.00            | <input checked="" type="checkbox"/> | <input checked="" type="checkbox"/> |
| 4  | <input checked="" type="checkbox"/> | CS03.Last Step  | Unknown | 1.00            | <input checked="" type="checkbox"/> | <input checked="" type="checkbox"/> |
| 5  | <input type="checkbox"/>            | CS04.Last Step  | 1.000   |                 | <input type="checkbox"/>            | <input type="checkbox"/>            |
| 6  | <input type="checkbox"/>            | CS05.Last Step  | 1.000   |                 | <input type="checkbox"/>            | <input type="checkbox"/>            |
| 7  | <input checked="" type="checkbox"/> | CS06.Last Step  | Unknown | 1.00            | <input checked="" type="checkbox"/> | <input checked="" type="checkbox"/> |
| 8  | <input checked="" type="checkbox"/> | CS07.Last Step  | Unknown | 1.00            | <input checked="" type="checkbox"/> | <input checked="" type="checkbox"/> |
| 9  | <input type="checkbox"/>            | CS08.Last Step  | 1.000   |                 | <input type="checkbox"/>            | <input type="checkbox"/>            |
| 10 | <input type="checkbox"/>            | CS09.Last Step  | 1.000   |                 | <input type="checkbox"/>            | <input type="checkbox"/>            |
| 11 | <input checked="" type="checkbox"/> | CS10.Last Step  | Unknown | 1.00            | <input checked="" type="checkbox"/> | <input checked="" type="checkbox"/> |
| 12 | <input type="checkbox"/>            | CS11.Last Step  | 1.000   |                 | <input type="checkbox"/>            | <input type="checkbox"/>            |
| 13 | <input type="checkbox"/>            | CS12.Last Step  | 1.000   |                 | <input type="checkbox"/>            | <input type="checkbox"/>            |
| 14 | <input type="checkbox"/>            | CS13.Last Step  | 1.000   |                 | <input type="checkbox"/>            | <input type="checkbox"/>            |
| 15 | <input checked="" type="checkbox"/> | CS14.Last Step  | Unknown | 1.00            | <input checked="" type="checkbox"/> | <input checked="" type="checkbox"/> |

☐ Simultaneous Equations Method

Select All Unselect All Get Unknown Load Factors OK Cancel

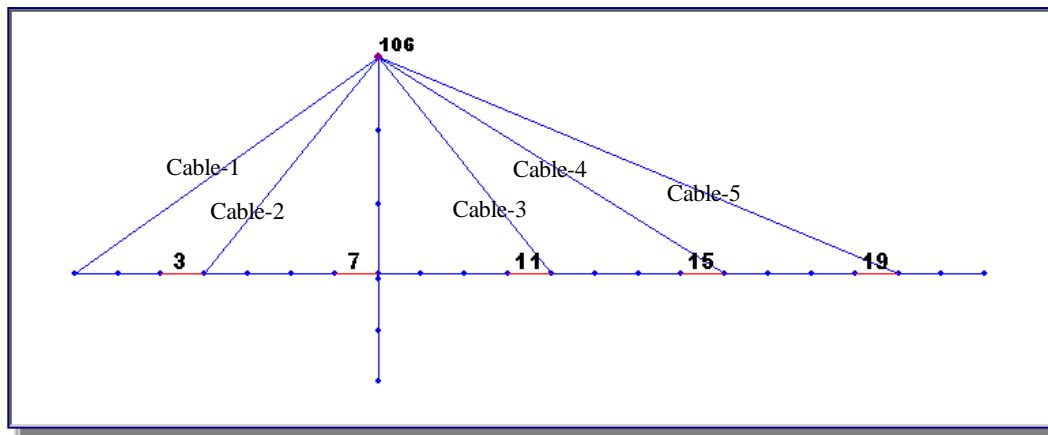
**Figure 5. Input data for Unknown Load Factors**

## Example of Unknown Load Factors using Forward Construction Stage Analysis

- Constrain bending moments of stringers, which are in contact with cables and the lateral displacement of the pylon at the final stage.

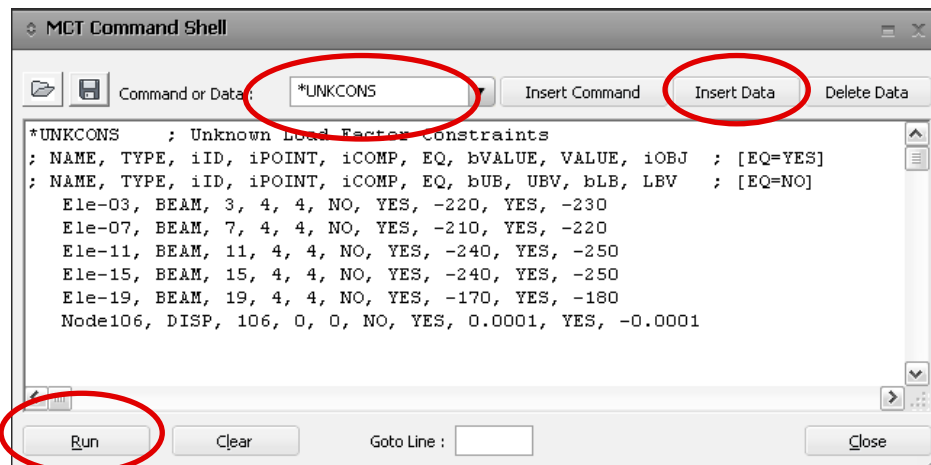
**Table 5. Constrained conditions for the example model**

|   | Constraint Name | Constraint Type | Element / Node | Point | Component | Inequality Condition |             |
|---|-----------------|-----------------|----------------|-------|-----------|----------------------|-------------|
|   |                 |                 |                |       |           | Upper Bound          | Lower Bound |
| 1 | Ele-03          | Beam Force      | 3              | J     | My        | -220                 | -230        |
| 2 | Ele-07          | Beam Force      | 7              | J     | My        | -210                 | -220        |
| 3 | Ele-11          | Beam Force      | 11             | J     | My        | -240                 | -250        |
| 4 | Ele-15          | Beam Force      | 15             | J     | My        | -240                 | -250        |
| 5 | Ele-19          | Beam Force      | 19             | J     | My        | -170                 | -180        |
| 6 | Node 106        | Displacement    | 106            | -     | DX        | 0.0001               | -0.0001     |



**Figure 6. Elements and a node to be constrained**

- Constraints can be readily modified using the MCT Command Shell feature. To display the entered constraints, input \*UNKCONS for Command or Data of Tools>MCT Command Shell, followed by clicking the Insert Data button. Modify or add data within the text window and then click on the Run button. This will reflect the modification or addition of constraints in the program.



**Figure 7. Modification or addition of constraints using MCT Command Shell**

## 8.5 Unknown Load Factors Results

Unknown load factors, which satisfy constraint conditions (bending moments of stringers and lateral displacements of pylons) specified at the final stage, are displayed in a table form, as shown in Figure 8.

|             | CS02/Last Step | CS03/Last Step | CS06/Last Step | CS07/Last Step | CS10/Last Step | CS14/Last Step |
|-------------|----------------|----------------|----------------|----------------|----------------|----------------|
| Factor      | 89.006         | 155.411        | 375.324        | 251.370        | 332.310        | 42.658         |
| Constraint  | Ele-03         | Ele-07         | Ele-11         | Ele-15         | Ele-19         | Node106        |
| Value       | -230.000       | -220.000       | -250.000       | -250.000       | -170.000       | 0.000          |
| Upper Bound | -220.000       | -210.000       | -240.000       | -240.000       | -170.000       | 0.000          |
| Lower Bound | -230.000       | -220.000       | -250.000       | -250.000       | -180.000       | -0.000         |

**Figure 8. Unknown Load Factors results**

**Table 6. Calculated loads at each construction stage**

| Classification           | Stage/Step | Entered unit load | Unknown load factor | Actual load  |
|--------------------------|------------|-------------------|---------------------|--------------|
| Pretension of Cable 2    | CS02/Last  | 1 tonf            | 89.006              | 89.006 tonf  |
| Pretension of Cable 3    | CS03/Last  | 1 tonf            | 155.411             | 155.411 tonf |
| Pretension of Cable 1    | CS06/Last  | 1 tonf            | 375.324             | 375.324 tonf |
| Pretension of Cable 4    | CS07/Last  | 1 tonf            | 251.370             | 251.370 tonf |
| Pretension of Cable 5    | CS10/Last  | 1 tonf            | 332.310             | 332.310 tonf |
| Jack Up at right support | CS14/Last  | 1 mm              | 42.658              | 42.658 mm    |

**Table 7. Results at the final stage (CS 14) after the calculated loads for each construction stage have been reflected**

| Classification | Bending moment of stringer |              |               |               |               | Unit: tonfm, m                |
|----------------|----------------------------|--------------|---------------|---------------|---------------|-------------------------------|
|                |                            |              |               |               |               | Lateral displacement of pylon |
| Location       | Element 3(J)               | Element 7(J) | Element 11(J) | Element 15(J) | Element 19(J) | Node 106                      |
| Final result   | -230.0                     | -220.0       | -250.0        | -250.0        | -170.0        | 0.0001                        |

## Example of Unknown Load Factors using Forward Construction Stage Analysis

Influence Matrix obtained from Unknown Load Factors is shown in Figure 9.

|                | Constraint  | Ele-03    | Ele-07    | Ele-11   | Ele-15   | Ele-19   | Node106   |
|----------------|-------------|-----------|-----------|----------|----------|----------|-----------|
|                | Upper Bound | -220.000  | -210.000  | -240.000 | -240.000 | -170.000 | 0.000     |
|                | Lower Bound | -230.000  | -220.000  | -250.000 | -250.000 | -180.000 | -0.000    |
|                | Value       | -230.000  | -220.000  | -250.000 | -250.000 | -170.000 | 0.000     |
| CS02/Last Step | 89.006      | -5.354529 | 0.000000  | 0.000000 | 0.000000 | 0.000000 | -0.000679 |
| CS03/Last Step | 155.411     | 1.398701  | 12.493900 | 0.000000 | 0.000000 | 0.000000 | 0.000177  |
| CS06/Last Step | 375.324     | 3.956726  | 1.592571  | 0.000000 | 0.000000 | 0.000000 | -0.000383 |
| CS07/Last Step | 251.370     | 0.625364  | 3.085723  | 8.479982 | 0.000000 | 0.000000 | 0.000009  |
| CS10/Last Step | 332.310     | 0.055038  | 0.316618  | 5.105819 | 6.153846 | 0.000000 | -0.000000 |
| CS14/Last Step | 42.658      | 0.693490  | 0.303872  | 1.620756 | 2.610336 | 1.663942 | -0.000073 |

Result Influence Matrix Iterative Analysis Generate Excel File OK

**Figure 9. Displaying Influence Matrix**

As shown in Figure 10, Influence Matrix obtained from Unknown Load Factors is convertible into an Excel sheet.

|    | A   | B           | C            | D                        | E            | F           | G            | H            |
|----|---|-------------|--------------|--------------------------|--------------|-------------|--------------|--------------|
| 1  |   |             |              |                          |              |             |              |              |
| 2  | <b>UnknownLoad Factor Result (Influence Matrix)</b> |             |              |                          |              |             |              |              |
| 3  |   |             |              |                          |              |             |              |              |
| 4  | File Name :   |             |              | Date : 2012/7/25         |              |             |              |              |
| 5  | Number of Constraints : 6                           |             |              | Number of Load Cases : 6 |              |             |              |              |
| 6  |   |             |              |                          |              |             |              |              |
| 7  |   |             |              |                          |              |             |              |              |
| 8  |   | Constraint  | Ele-03       | Ele-07                   | Ele-11       | Ele-15      | Ele-19       | Node106      |
| 9  | Factor  | Upper Bound | -220         | -210                     | -240         | -240        | -170         | 0.0001       |
| 10 |   | Lower Bound | -230         | -220                     | -250         | -250        | -180         | -0.0001      |
| 11 |   | Value       | -229.9998998 | -220.0000274             | -249.9999778 | -249.999989 | -170.0000022 | 9.99319E-05  |
| 12 | CS02/Last Step                                      | 89.00637817 | -5.354528692 | 0                        | 0            | 0           | 0            | -0.000679016 |
| 13 | CS03/Last Step                                      | 155.4107819 | 1.398700896  | 12.49389989              | 0            | 0           | 0            | 0.000177371  |
| 14 | CS06/Last Step                                      | 375.3236389 | 3.956726365  | 1.592571261              | 0            | 0           | 0            | -0.000382734 |
| 15 | CS07/Last Step                                      | 251.3700409 | 0.625364259  | 3.085723262              | 8.479982435  | 0           | 0            | 9.28018E-06  |
| 16 | CS10/Last Step                                      | 332.3103027 | 0.055038218  | 0.316618374              | 5.105818747  | 6.153845768 | 0            | -3.15178E-07 |
| 17 | CS14/Last Step                                      | 42.65824509 | 0.693490187  | 0.303871508              | 1.620756086  | 2.610335862 | 1.663942192  | -7.34581E-05 |

**Figure 10. Influence Matrix converted into an Excel sheet**

## 8.6 Construction Stage Analysis

Load factors calculated from Unknown Load Factors are reflected in the staged construction model and the re-analyzed results are shown in Figure 11 and 12.

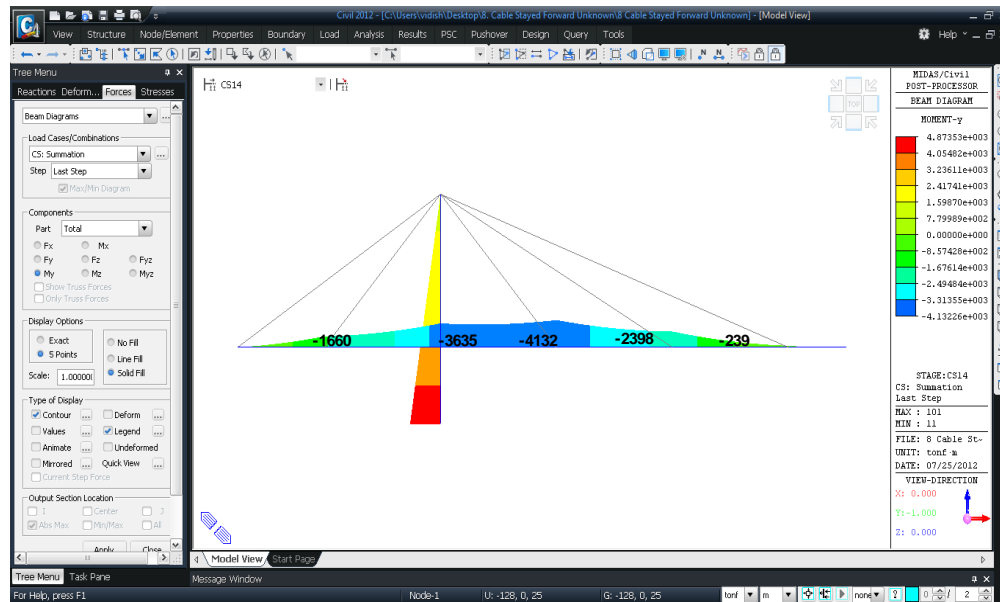


Figure 11. Bending moments at the final stage (CS14)

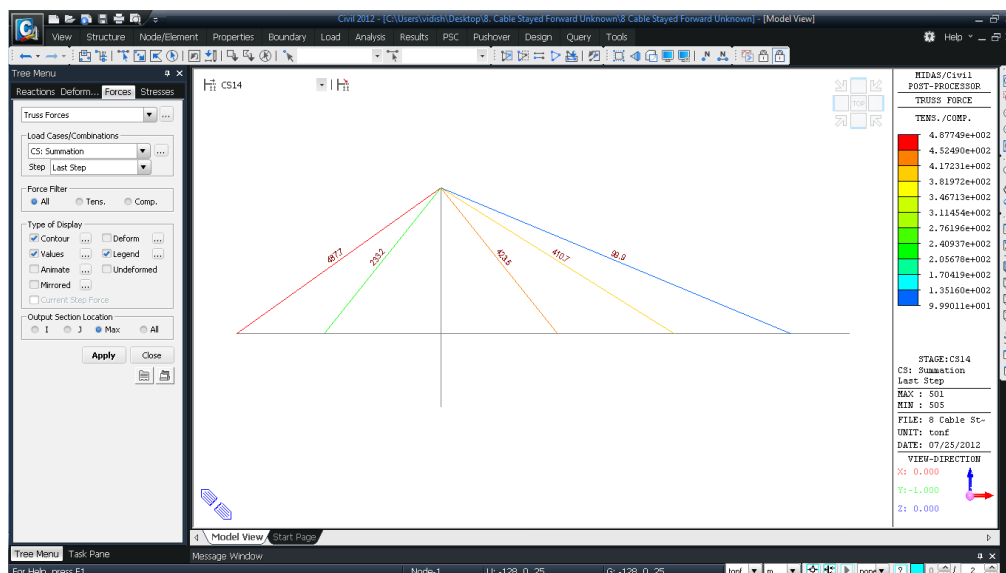


Figure 12. Cable axial forces at the final stage (CS14)

(1) Bending moments at each construction stage

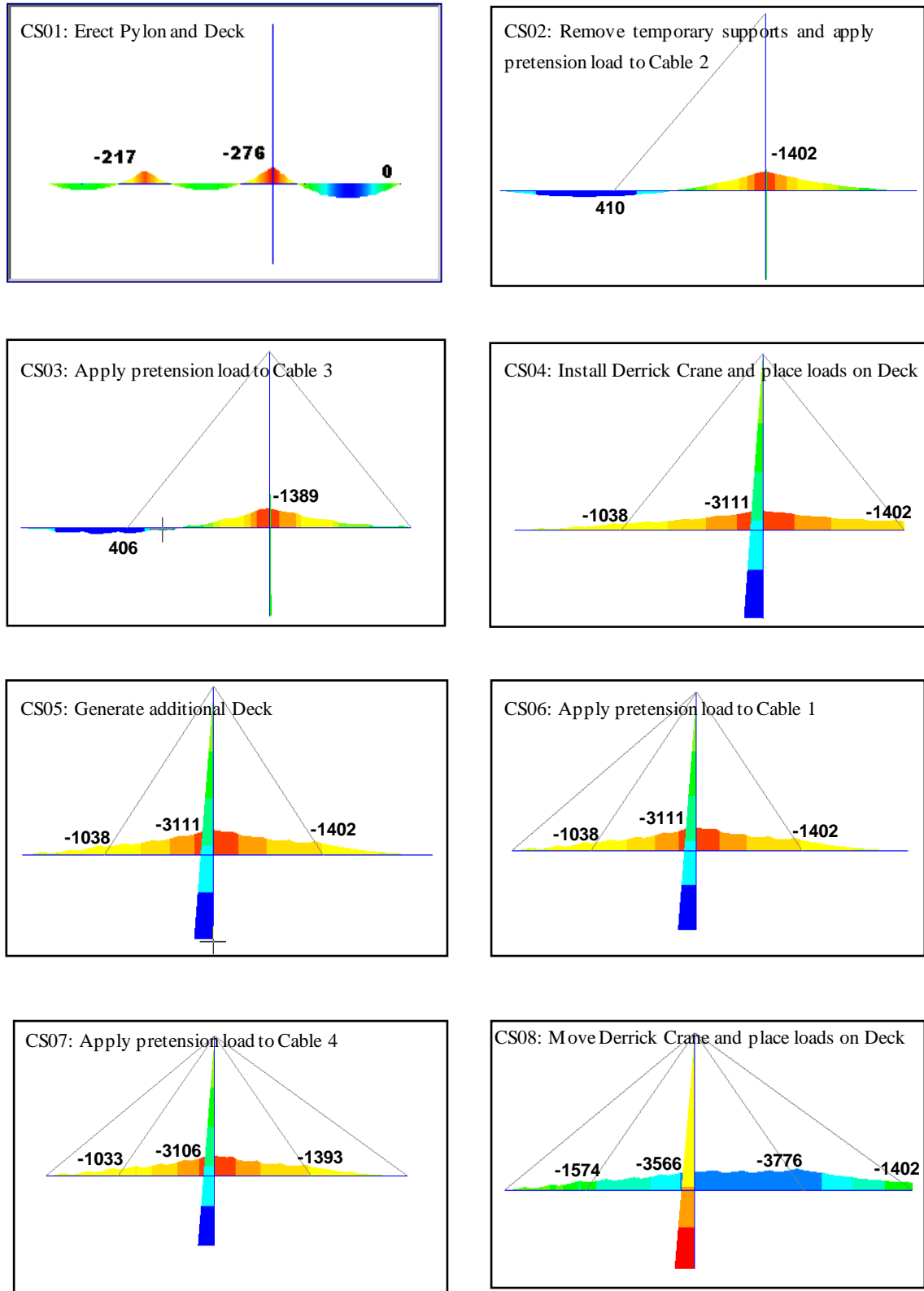


Figure 13-A. Bending moments at each construction stage (CS01~CS08)

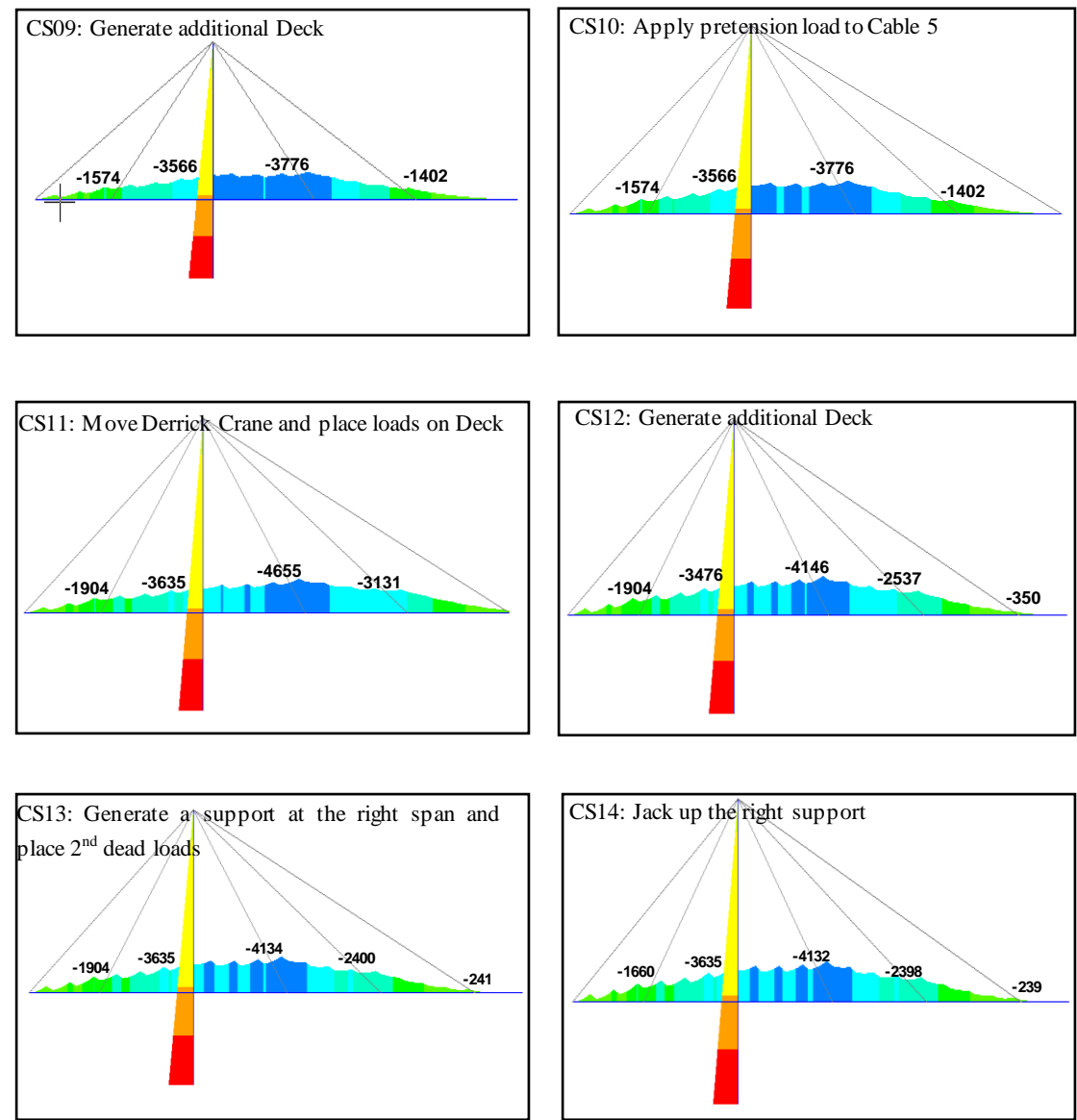


Figure 13-B. Bending moments at each construction stage (CS09~CS14)